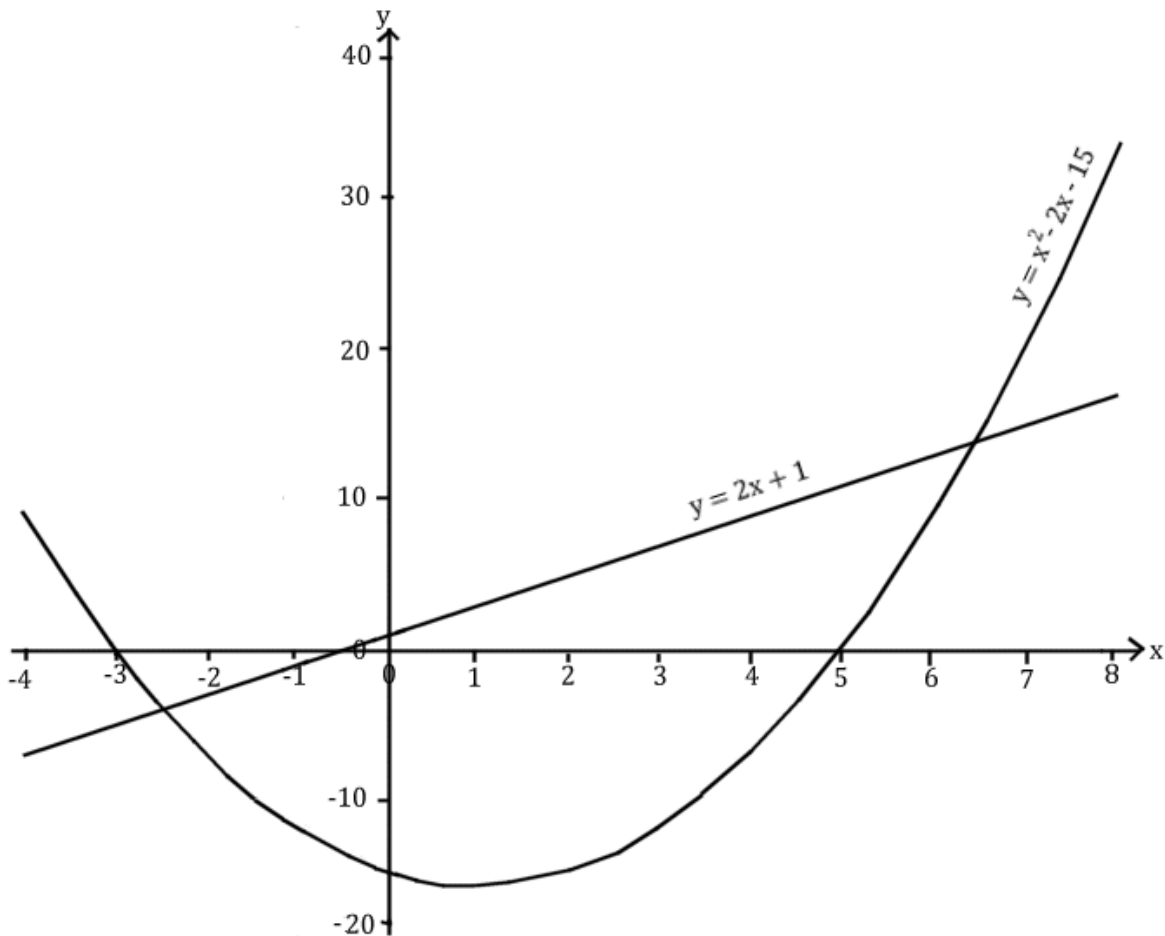


Solving Quadratic Equations - ANSWERS

1.



2. The intercepts with the x-axis are at -3 and 5

$$\begin{aligned} 3. \quad x^2 - 2x - 15 &= 0 \\ (x + 3)(x - 5) &= 0 \\ x + 3 &= 0 \quad \text{or} \quad x - 5 = 0 \\ x &= -3 \quad \text{or} \quad x = 5 \end{aligned}$$

$$\begin{aligned} 4. \quad x^2 - 2x - 15 &= 0 \\ x^2 - 2x + 1 - 15 - 1 &= 0 \\ (x - 1)^2 - 16 &= 0 \\ (x - 1)^2 &= 16 \\ x - 1 &= \pm 4 \\ x - 1 &= -4 \quad \text{or} \quad x - 1 = 4 \\ x &= -3 \quad \text{or} \quad x = 5 \end{aligned}$$

5. Substituting in the formula $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$\begin{aligned} x &= \frac{-(-2) \pm \sqrt{2^2 - 4 \times 1 \times -15}}{2 \times 1} \\ x &= \frac{2 \pm \sqrt{4 - (-60)}}{2} \\ x &= \frac{2 \pm \sqrt{64}}{2} \\ x &= \frac{2-8}{2} \quad \text{or} \quad x = \frac{2+8}{2} \\ x &= -3 \quad \text{or} \quad x = 5 \end{aligned}$$

$$6. \quad x^2 - 4x - 16 = 0$$

If $2x + 1$ is added to both sides of the equation like this: $x^2 - 4x - 16 + 2x + 1 = 2x + 1$ it gives: $x^2 - 2x - 15 = 2x + 1$

So, if we draw the graph of $y = 2x + 1$ on the same axes as $y = x^2 - 2x - 1$, where the curves intersect it will be true that:

$$x^2 - 2x - 15 = 2x + 1$$

and that:

$$x^2 - 4x - 16 = 0$$

7. Substituting in the formula $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$x = \frac{-(-4) \pm \sqrt{4^2 - 4 \times 1 \times -16}}{2 \times 1}$$

$$x = \frac{4 \pm \sqrt{4 - (-64)}}{2}$$

$$x = \frac{4 \pm \sqrt{80}}{2}$$

$$x = \frac{4-8.9}{2} \quad \text{or} \quad x = \frac{4+8.9}{2}$$

$$x = \frac{-4.9}{2} \quad \text{or} \quad x = \frac{12.9}{2}$$

$$x = -2.45 \quad \text{or} \quad x = 6.45$$

(Confirm that your graphical solution is correct.)